

Memetic search for composing medical crews with equity and efficiency

Qing Zhou ^a, Jin-Kao Hao ^{a,b}, Zhe Sun ^c, Qinghua Wu ^{c,*}

^a*LERIA, Université d'Angers, 2 bd Lavoisier, 49045 Angers, France
email: qingzhou@hust.edu.cn; jin-kao.hao@univ-angers.fr*

^b*Institut Universitaire de France, 1 rue Descartes, 75231 Paris, France*

^c*School of Management, Huazhong University of Science and Technology, No.
1037, Luoyu Road, Wuhan, China
email: qinghuawu1005@gmail.com*

Applied Soft Computing, May 2020 (In Press)

Abstract

Composing medical crews with equity and efficiency is an important practical problem commonly arising from health care system management. This work presents the first hybrid memetic algorithm for this problem. The proposed approach integrates an original backbone-based crossover for generating promising offspring solutions and a tabu search based local optimization algorithm exploring both feasible and infeasible search regions. Computational experiments on two sets of benchmark instances in the literature are conducted to assess the proposed algorithm with reference to existing methods. This study advances the state-of-the-art of solving this relevant practical problem and is expected to inspire new solution methods to similar problems.

Keywords: Health care service management; memetic algorithm; hybrid search; tabu search; heuristics.

1 Introduction

The quality of medical services critically depends on the delivery of health care and is directly connected to the equity and the efficiency of the health care system. Efficiency mainly concerns providing high quality health care services,

* Corresponding author.

while equity mainly refers to the access to health care systems which should be fairly given to all citizens regardless of age, gender, income and residence.

In general, health care is delivered by medical crews composed of practitioners working together by sharing their skills, experience and knowledge. Among the important issues in health care service management, the pre-hospital care provided by the Emergency Medical Services (EMS) is primordial critical [1]. EMS is responsible for providing timely and appropriate first aid services in case of emergency situations such as accidents. The purpose of such services is to reduce patient death, prevent disability and increase the likelihood of recovery [3]. In [5], Aringhieri presented the first study of the problem of composing medical crews such that the health care service provided complies with the equity and efficiency principles. This problem naturally arises in health care service management, such as building crews for heart surgery or other specific surgeries. A real case from the operation center of the Emergency Medical Service of Milan is described in [4], where the operation center deals with each demand (emergency call) in a timely manner and for urgent calls the response must be fulfilled in less than 8 minutes in the urban regions according to the Italian law. Generally, this problem can be used as a model to formulate practical problems in other settings, such as composing suitable teams with different skills and knowledge that are assigned to a new project.

The problem of composing medical crews with equity and efficiency (CMCEE) studied in this work can be described as follows [5]. Given a set of n individuals $N = \{1, \dots, n\}$, for each individual $p \in N$, its efficiency is modeled with a positive value $e_p \in \mathbb{R}^+$ which represents the proficiency of individual p to do a job. Skill difference between two individuals p and q is modeled by a value $d_{pq} \in \mathbb{R}^+$ ($p, q \in N$, $d_{pq} = d_{qp}$ and $d_{pp} = 0$) representing how much the skills of p and q are heterogeneous. The problem is to select a subset of individuals to compose T (T is given) distinct crews such that each crew t ($t = 1, \dots, T$) has exactly M_t individuals and the skill diversity of each crew is guaranteed to attain a diversity threshold D_{min} while the efficiency of the crew with the smallest efficiency is maximized.

Formally, the CMCEE can be expressed as the following mathematical model with each binary variable $x_{pt} = 1$ ($p = 1, \dots, n$, $t = 1, \dots, T$) if the individual p is allocated to crew t and $x_{pt} = 0$ otherwise [5,9]:

$$\text{maximize} \quad \min_{t=1, \dots, T} \sum_{p=1}^n e_p x_{pt} \quad (1)$$

$$\text{subject to} \quad \sum_{t=1}^T x_{pt} \leq 1, \quad p = 1, \dots, n \quad (2)$$

$$\sum_{p=1}^n x_{pt} = M_t, \quad t = 1, \dots, T \quad (3)$$

$$\sum_{p=1}^{n-1} \sum_{q=p+1}^n d_{pq} x_{pt} x_{qt} \geq D_{min}, \quad t = 1, \dots, T \quad (4)$$

$$x_{pt} \in \{0, 1\}, \quad p = 1, \dots, n, \quad t = 1, \dots, T \quad (5)$$

where the objective (1) commits to maximize the efficiency of the crew with the smallest efficiency. Constraint (2) guarantees that each individual is allocated to at most one crew and constraint (3) ensures that the cardinality of crew t is exactly M_t , while constraint (4) forces the sum of skill differences of each crew to be at least D_{min} .

As the literature review of Section 2 shows, there are a number of studies to address the issue of tradeoff between equity and efficiency of health care service management. In addition to its practical relevance, the CMCEE is known to be NP-hard [5] and consequently computationally challenging. Given that exact methods will have an exponential time complexity on the size of the problem, this work focuses thus on developing effective heuristic methods for the CMCEE able to find high-quality solutions with a reasonable time frame. The main contributions of this work are summarized as follows.

- This work presents the first population-based memetic algorithm (MA) for solving the CMCEE, which possesses two original features. First, it integrates an original crossover operator for generating promising offspring solutions. The crossover operator maximally preserves common individuals ('building blocks') grouped in the same crew of parent solutions and favors the inheritance of desirable 'building blocks' through the recombination process. Second, the proposed algorithm uses an effective local optimization procedure combining feasible and infeasible searches driven by the following consideration. By relaxing the diversity threshold constraint in a controlled manner, the algorithm is able to tunnel through feasible and infeasible regions to locate high quality solutions which are difficult to attain otherwise.
- Computational experiments on two sets of benchmark instances in the literature show the competitiveness of the proposed algorithm with respect to existing methods. This implies that our method is able to compose medical crews with a higher equity and a better efficiency. Moreover, the code of our algorithm will be publicly available, which can serve as an useful tool for researchers and practitioners in health care service management. Finally, as the underlying search strategies of the proposed method are rather general, they can be beneficially adapted to similar settings where equity and efficiency are to be considered.

The rest of the paper is structured as follows. Section 2 presents a detailed

review of related works on the studied problem. Section 3 shows the general framework of the proposed algorithm, while its two key search components (crossover and local optimization) are presented in Sections 4 and 5, respectively. Section 6 is dedicated to computational assessments of the proposed algorithm and comparisons with the best performing algorithms in the literature, followed by an experimental analysis of the key components of the algorithm in Section 7. Conclusions are drawn in Section 8.

2 Related works

This section presents a detailed review of the related studies on the composing medical crews with equity and efficiency problem (CMCEE), which originates from a real application from the health care service management. Since the 80s, several studies have considered the issue of efficiency and equity or fairness in health care services.

Mayhew and Leonardi [22] proposed a model that enables a tradeoff between equity and efficiency with application to a regional health-care resource allocation problem in London. Cho [8] presented an equity-efficiency tradeoff model for the location of medical care facilities where equity is represented by the chance to receive medical services whereas efficiency is represented by consumer and producer welfare. Aringhieri [5] proposed both a mathematical model and a graph model following the principles of equity and efficiency that arises from the EMS system of Milan [4]. The author also proposed an effective heuristic algorithm (denoted as GTS) by hybridizing a greedy initialization procedure, a local improvement method and a tabu search procedure. Within GTS, the local improvement method confines its search process in feasible regions, while the tabu search method is allowed to visit infeasible solutions by using a penalized evaluation function. Experimental results showed that the GTS algorithm was able to achieve much better results than the commercial solver Cplex with a shorter computation time. Later, Smith et al. [30] introduced a series of hierarchical location models with bi-objectives (efficiency and equity) for a public service application. Khodaparasti et al. [18] presented an integrated location-allocation model that considers both efficiency and equity for an EMS application. More recently, Delgado-Osuna et al. [9] developed an artificial bee colony (ABC) algorithm for the CMCEE, which deals with infeasible solutions by using a destructive-constructive neighborhood operator and a specialized local search procedure. The reported computational results showed that ABC outperformed the reference algorithms GGA [9] and GTS [5]. Artificial bee colony is a relative new population-based algorithm inspired by the foraging behavior of honeybees. Although ABC has been successfully used in many problems [17] due to its simplicity, it may suffer from the problem of premature

convergence and getting stuck on local optima easily in some scenarios. Recently, Abualigah et al. [2] reviewed sentiment analysis methods and techniques in the health care management to improve health care quality.

According to the computational studies reported in the literature on the CMCEE, the GTS algorithm [5] and the ABC algorithm [9] represent the state of the art of solving the CMCEE. Meanwhile, it is known that the population-based memetic search framework is among the most powerful general methods for grouping problems such as graph coloring [11,16,26], graph partitioning [7,12] and bin packing [10]. Until now, this approach remains unexplored for the CMCEE. This work aims thus to fill the gap by investigating for the first time the potential of the memetic search framework for solving the CMCEE. As the computational results (Section 6) demonstrate, this approach is indeed very successful by finding many improved best solutions for a majority of the tested CMCEE benchmark instances available in the literature.

3 Memetic algorithm for the CMCEE

3.1 General procedure

Memetic algorithms are a powerful and general framework for difficult combinatorial optimization problems [24]. Typically, a memetic algorithm promotes the idea of combining the diversification power of population-based evolutionary search and the intensification strength of local search optimization [14]. The flowchart (Fig. 1) illustrates the general procedure of our proposed memetic algorithm (MA) for the problem of composing medical crews with equity and efficiency. As Algorithm 1 (see Appendix) shows, MA starts with an initial population where each solution is produced by a greedy construction algorithm (Section 3.2). Then the algorithm enters the ‘while’ loop to perform a number of evolutionary generations until a given cutoff time limit is reached. At each generation, MA selects two parents at random from the population, which are recombined by the backbone-based crossover operator (Section 4) to generate an offspring solution. Subsequently, the generated offspring is improved by the feasible and infeasible tabu search algorithm (Section 5). Finally, the improved offspring solution is used to update the population (Section 3.3).

The remaining of this section is dedicated to population initialization and its update while the crossover operator and the local optimization procedure are presented in two other sections. As it will be evidenced, compared to the two leading CMCEE algorithms (i.e., the tabu search algorithm [5] and the artificial bee colony algorithm [9]), our approach relies on a

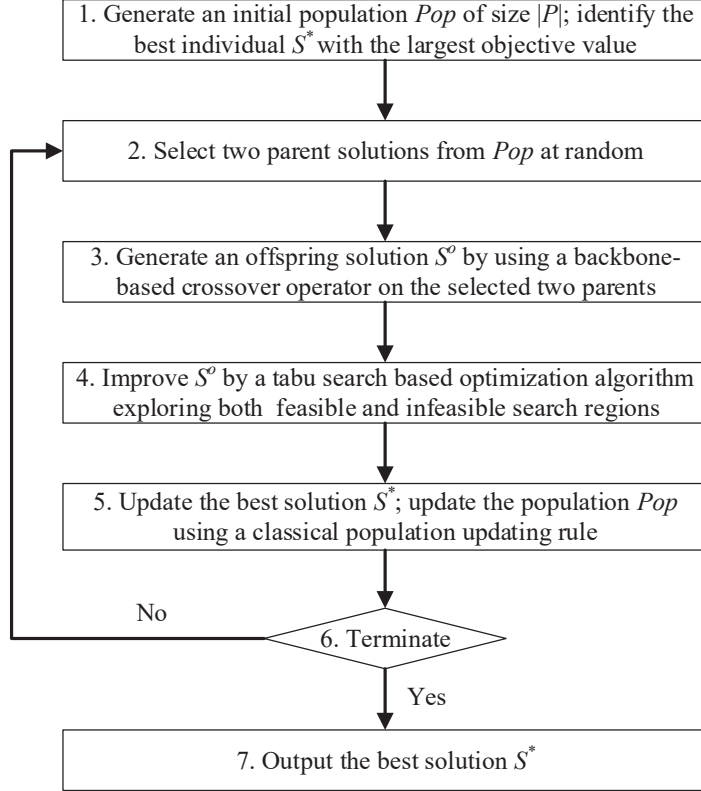


Fig. 1. Flowchart of the proposed MA algorithm.

different search framework (i.e., memetic search) and integrates different search components (i.e., crossover, specific local optimizer), leading to a very competitive algorithm.

3.2 Population initialization

The $|P|$ initial solutions of the population are generated by applying the greedy construction algorithm (denoted as GC, see Algorithm 2 of the Appendix) proposed in [5]. Let S denote a candidate solution which is a set of $T+1$ crews $S = \{C_0, C_1, \dots, C_T\}$ such that each C_t ($t \in \{1, \dots, T\}$) is the set of individuals allocated to crew t while $C_0 = \{1, \dots, n\} \setminus \{C_1 \cup \dots \cup C_T\}$ is a dummy crew containing the unallocated individuals. To ensure an efficient implementation of the GC algorithm, a matrix B with its element B_{pt} is used to represent the diversity contribution of each individual p to any crew t [5], where each B_{pt} sums up the diversities between p and all members allocated to C_t :

$$B_{pt} = \sum_{q \in C_t} d_{pq}, q \neq p, p \in \{1, \dots, n\}, t \in \{1, \dots, T\} \quad (6)$$

Initially, $C_0 = \{1, \dots, n\}, C_t = \emptyset$ ($t \in \{1, \dots, T\}$) and $B_{pt} = 0$ ($p \in \{1, \dots, n\}, t \in \{1, \dots, T\}$). Then at each construction step, GC considers all unallocated individuals having the largest efficiency and all incomplete crews with minimum members. Among all these individuals and crews, GC allocates a member p to a crew C_t ($t \in \{1, \dots, T\}$) such that the diversity contribution B_{pt} is maximized. This process is repeated until all the crews are complete. Note that the solution constructed by GC always guarantees the feasibility of the cardinality constraint (Constraint (3)) but it may violate the diversity threshold constraint that the sum of skill diversity of each crew must satisfy a certain threshold. In this case, the solution repair procedure (Section 5.4) is applied to transform the infeasible solution S into a feasible one.

3.3 Population updating strategy

A classical population updating rule is used to decide whether the offspring solution after the tabu search improvement should be inserted into the population or not. If the offspring solution is different from the solutions of the population and has a better objective value than the worst solution in the population, then the offspring replaces the worst solution in the population. Otherwise the offspring is discarded and the population is kept unchanged.

4 Crossover operator

The crossover operator of our MA algorithm plays a critical role of diversification and aims at leading the search process to new promising search areas. As indicated in [14], a successful crossover operator should be able to transfer meaningful features from parent solutions to offspring solutions. To design a semantic crossover operator for the CMCEE, the studied problem is considered as a grouping problem whose purpose is to seek a particular partition of n individuals into $T + 1$ crews (groups). For grouping problems, it is preferable and natural for a crossover to handle groups of individuals rather than individuals. Crossover operators based on this idea have been successfully used to solve several grouping problems [10,11,16,26]. In case of the CMCEE, a preliminary analysis (Section 7.2) discloses that high quality solutions always contain crews that share the same individuals across the solutions. It thus can be expected that these shared individuals also have a high chance to stay together in the global optimum. Following this consideration, the main idea of our crossover operator is to preserve the groupings of individual (backbone) from parent solutions to offspring solutions.

The proposed backbone-based crossover operator (denoted as BCX) generates

an offspring solution from two parent solutions selected at random.

Definition 1 (backbone): Given two parent solutions $S^1 = \{C_0^1, C_1^1, \dots, C_T^1\}$ and $S^2 = \{C_0^2, C_1^2, \dots, C_T^2\}$, the backbone BB of S^1 and S^2 is the set of T subsets of individuals $\{BB_1, \dots, BB_T\}$ such that each BB_i , $i \in \{1, \dots, T\}$ is the subset of individuals that are grouped together in both S^1 and S^2 , i.e., $\exists m, n \in \{1, \dots, T\}$, $BB_i = C_m^1 \cap C_n^2$, while the size of $BB_1 \cup \dots \cup BB_T$ is as large as possible.

Note that the backbone definition does not take into account the set of unallocated individuals of the parent solutions since they are typically low-efficiency and have a small chance to be part of high quality solutions. Based on the notion of backbone, BCX considers, for both parent solutions, only the T crews of allocated individuals.

Definition 2 (individual contribution): Given a solution $S = \{C_0, C_1, \dots, C_T\}$, the individual contribution of a member p ($p \in \{1, \dots, n\}$) to a crew t ($t \in \{1, \dots, T\}$) of S is defined by taking into consideration both its efficiency and its diversity contribution to crew t :

$$IC(S, p, t) = e_p * \sum_{q \in C_t, q \neq p} d_{pq} \quad (7)$$

Based on the backbone, the proposed BCX crossover generates an offspring $S^o = \{C_0^o, C_1^o, \dots, C_T^o\}$ in two steps as illustrated in Algorithm 3 of the Appendix. The first step is to create a partial solution based on the backbone of the two selected parent solutions while the second step is to complete the partial solution by allocating some of the unallocated individuals.

Create a partial solution based on backbone. To create a partial offspring solution based on the backbone, it is necessary to carry out a group matching procedure that aims to determine a proper matching between the crews of the two parents, such that it can preserve as many common individuals grouping together in both parent solutions as possible. This group matching problem can be solved by the classic Hungarian approach [19]. However, this will be too time consuming in our case since a maximum weight matching is needed for each crossover application. Therefore, a fast group matching algorithm is adopted to find a near-optimal matching between the crews of the two parent solutions which is used to create a partial solution. The group matching algorithm builds the partial offspring solution S^o in T steps (lines 4-8), and each step t ($t = 1, \dots, T$) constructs a crew C_t^o of allocated individuals for S^o as follows. It first identifies a crew C_i^1 , $i \in \{1, \dots, T\}$ of S^1 and a crew C_j^2 , $j \in \{1, \dots, T\}$ of S^2 (line 7) such that C_i^1 and C_j^2 have the largest number of identical individuals across all $i \in \{1, \dots, T\}$ and $j \in \{1, \dots, T\}$, i.e., $\max_{i \in \{1, \dots, T\}, j \in \{1, \dots, T\}} |C_i^1 \cap C_j^2|$. For each identified pair of matched crews, one

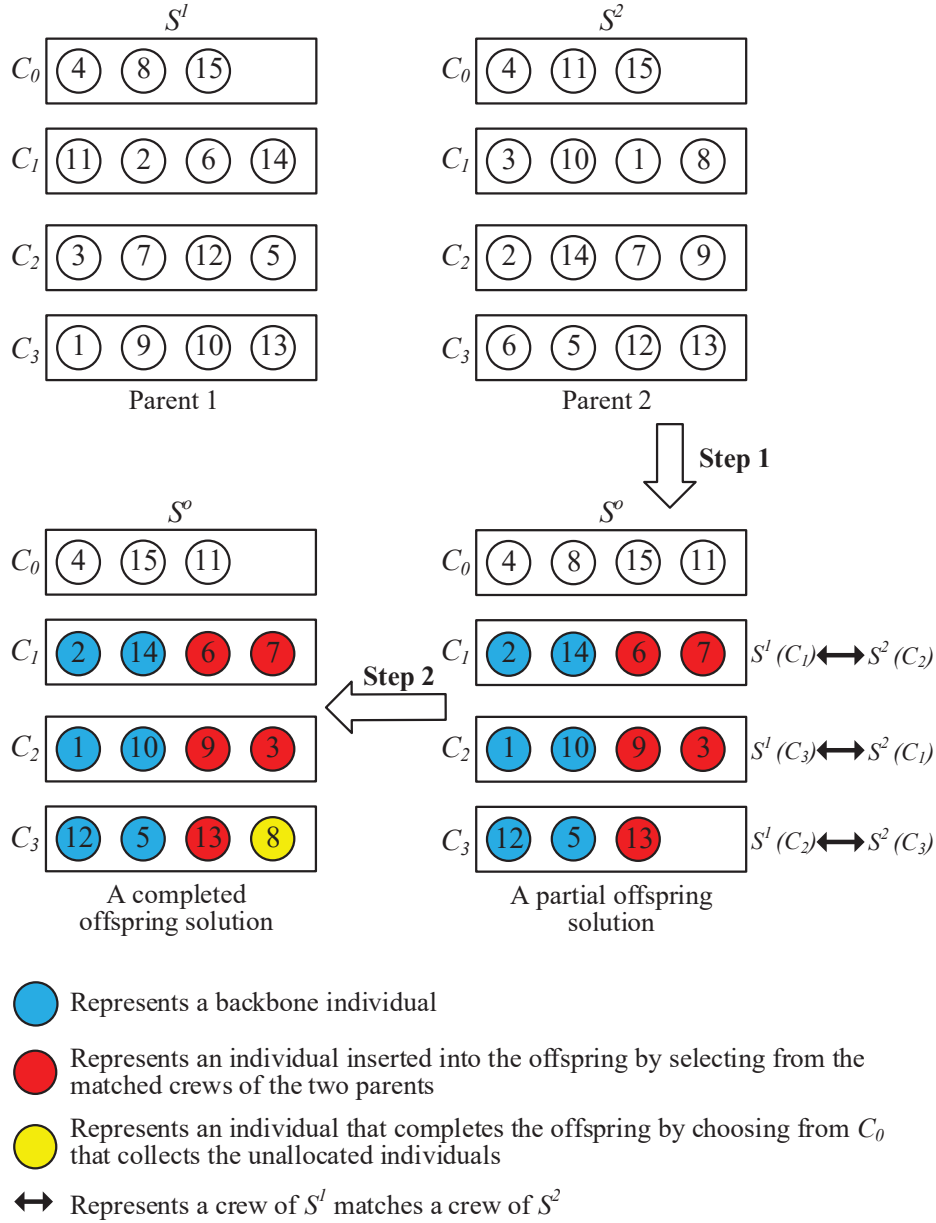


Fig. 2. An illustrative example of backbone crossover steps.

first preserves the backbone (i.e., all common individuals) to the corresponding crew of the offspring solution (line 8), i.e., $C_t^o = C_i^1 \cap C_j^2$. Then, C_t^o is further extended by inserting the remaining individuals in C_i^1 and C_j^2 (lines 10-20). Precisely, let $L_1 = C_i^1 \setminus C_t^o$ and $L_2 = C_j^2 \setminus C_t^o$ respectively denote the remaining individuals in C_i^1 and C_j^2 (line 10), the extending procedure alternatively chooses an individual m with the highest individual contribution from L_1 in odd steps and from L_2 in even steps (lines 12-16). Once the selected individual is inserted to C_t^o (line 17), it is removed from the respective set L_1 or L_2 (line 18). This process is repeated until the number of members in C_t^o reaches M_t or both sets L_1 and L_2 become empty. At the end of step t , all individuals in

C_t^o are removed from all crews of both parents (line 20).

Complete the partial solution. A greedy construct algorithm is applied to complete the partial offspring solution which performs a series of insertion operations until the cardinality of each crew t of S^o reaches M_t (lines 22-27). Let L designate the subset of all remaining unallocated individuals after the first step. At each iteration, the greedy algorithm first selects an individual p from L producing the largest individual contribution $IC(S^o, p, t)$ to a crew t among the ones having the minimum cardinality. Then the selected individual p is displaced from L to crew t of the offspring S^o . Note that the obtained offspring solution after these steps may be an infeasible one violating the diversity threshold constraint. If this happens, a simple solution repair procedure (Section 5.4) is applied to transform the resulting solution into a feasible one (lines 28-30), which is then submitted to the tabu search method for further improvement (Section 5).

Fig. 2 shows an example to illustrate the main steps of the backbone-based crossover operator. There are 15 individuals which are grouped into 3 crews with 4 individuals per crew and one crew with 3 individuals. Given two parent solutions S^1 , S^2 , the offspring solution S^0 is created from the parents in two steps. First, the group matching algorithm is used to find the matched crews of S^1 and S^2 , and then each crew of the offspring solution is built by preserving the backbone individuals (individuals colored in blue), and is extended by inserting individuals with the highest individual contribution (individuals colored in red) selected alternately from the matched groups of S^1 and S^2 . For instance, since $S^1(C_1)$ matches $S^2(C_2)$ with two backbone individuals 2 and 14, these individuals are preserved in the offspring $S^0(C_1)$. Then individual 6 from $S^1(C_1)$ and 7 from $S^2(C_2)$ are selected to complete crew C_1 of the offspring. The other crews of S^0 are created in a similar way, while noting that C_3 is completed in the second step by including the unallocated individual with the highest contribution (8, indicated in yellow) from C_0 in S^0 that collects its unallocated individuals.

5 Tabu search with feasible and infeasible exploration

5.1 Main framework

Apart from the backbone based crossover, the local optimization procedure constitutes another critical component of our MA approach. As observed in many studies on strongly constrained problems [23,25,27,31], considering intermediary infeasible solutions during the search process may help to better explore the search space, because doing this may facilitate transitions between

structurally different solutions. Following this idea, the proposed tabu search algorithm (denoted as FITS) alternates between a feasible local search phase (denoted as FLS) where only feasible solutions are examined, and an infeasible local search phase (denoted as ILS) which permits a controlled exploration of infeasible solutions. These two local search phases play different roles in the FITS procedure. FLS is applied to intensify the search by focusing on the most relevant feasible solutions, while ILS is applied to diversify the search by introducing more search freedom through constraint relaxation.

The main framework of FITS is given in Algorithm 4 of the Appendix. Beginning with a feasible solution, FITS first performs the feasible local search phase ensured by the FLS procedure. The FLS procedure is based on the general tabu search framework [13] and relies on the exchange move operator to explore the most relevant feasible search space (Section 5.2). It stops when the best solution cannot be improved for N_{cons} consecutive iterations (N_{cons} is called the search depth of FLS). In this case, the search is considered to be stagnating and switches to the infeasible local search phase to bring more search freedom by relaxing the diversity threshold constraint in a controlled manner. The ILS procedure, which is also based on tabu search, relies on a penalty-based evaluation function to guide the search for an effective examination of the infeasible search space. It stops when a fixed number of iterations M_{ILS} is reached. The FITS procedure iterates these two complementary phases until an allowed maximum number of iterations β_{max} is reached. Computational results (see Section 7.1) indicate that the combined use of these complementary phases constitutes a highly effective hybridization for obtaining high quality solutions.

5.2 The feasible local search phase

The feasible local search procedure (FLS) aggressively examines the feasible search regions to seek improved solutions. This is achieved by using the following exchange move operator.

5.2.1 The Exchange move operator and solution evaluation

Given a feasible solution $S = \{C_0, C_1, \dots, C_T\}$, the exchange move swaps two individuals from different crews. To make the search more focused, FLS uses a constrained exchange move (denoted by $Exchange(p, q)$) [5,9] that exchanges an individual p from the crew C_w ($w > 0$) having the smallest efficiency with another individual q from a different crew C_t ($t \geq 0$). Notice that C_0 represents a dummy crew containing the unallocated individuals, and using C_0 in an exchange move enables the swap of an allocated individual and an

unallocated individual. For a fast calculation of the objective function of a candidate solution S' induced by swapping $p \in C_w$ and $q \in C_t$, a T -dimensional vector $E = \{E_1, \dots, E_T\}$ is used where $E_i = \sum_{k \in C_i} e_k$ denotes the efficiency of crew C_i . Since an exchange move only involves two crews, the efficiency of C_w (C_t) in S' can be easily computed as $E_w - e_p + e_q$ ($E_t - e_q + e_p$) with E . Similarly, to quickly verify the feasibility of the diversity threshold constraint of the candidate solution S' , a T -dimensional vector $D = \{D_1, \dots, D_T\}$ is maintained where $D_i = \frac{1}{2} \sum_{m, n \in C_i} d_{mn}$ denotes the total diversity of crew C_i , and hold a matrix B with $B_{pt} = \sum_{q \in C_t} d_{pq}$ representing the diversity contribution of individual p to a given crew t . With D and B , the diversity of C_w (C_t) in S' can be easily calculated as $D_w - B_{pw} + B_{qw} - d_{pq}$ ($D_t + B_{pt} - B_{qt} - d_{pq}$), and the verification of the feasibility of S' can be achieved in $O(1)$.

After performing an exchange move involving $p \in C_w$ and $q \in C_t$, the efficiency and diversity of the two crews can be conveniently updated by the following equations [5,9]:

$$E_w = E_w - e_p + e_q \quad (8)$$

$$E_t = E_t - e_q + e_p \quad (9)$$

$$D_w = D_w - B_{pw} + B_{qw} - d_{pq} \quad (10)$$

$$D_t = D_t + B_{pt} - B_{qt} - d_{pq} \quad (11)$$

Meanwhile, the diversity contribution of each individual with respect to crews w and t can be updated as follows [5,9]:

$$B_{rw} = B_{rw} - d_{pr} + d_{qr}, r \in \{1, \dots, n\} \quad (12)$$

$$B_{rt} = B_{rt} - d_{qr} + d_{pr}, r \in \{1, \dots, n\} \quad (13)$$

Therefore, for each performed exchange move, the matrix B is updated in $O(n)$, while the vector E and D are updated in $O(1)$.

5.2.2 Exploration with feasible local search

The tabu search based FLS procedure is summarized in Algorithm 5 of the Appendix. Starting from an initial input solution, FLS iteratively replaces the current solution S by a best admissible feasible neighboring solution S' obtained by applying the constrained exchange move operator. To avoid a short-term search cycling, each time an individual p is removed from its original crew t , it is forbidden to bring p back to crew t for the next tt iterations, where tt is a parameter called tabu tenure. A move is considered to be admissible if it is not forbidden by the tabu list or it produces a solution better than the best solution ever found during the search (aspiration criterion). Meanwhile, the best solution found is updated whenever an improved solution is obtained. The search stops when the best solution cannot

be updated for N_{cons} consecutive iterations where N_{cons} is the search depth of FLS. At this point, the search is deemed to be trapped into a deep local optimum and then it switches to the ILS phase to unlock the situation.

5.3 Infeasible local search phase

The basic idea behind ILS is to allow the algorithm to visit intermediary infeasible solutions by relaxing the diversity threshold constraint and enable the algorithm to visit an enlarged search space including both feasible and infeasible solutions. Following the general idea of penalty function for constrained optimization, ILS uses an extended penalty-based evaluation function F to evaluate the quality of both feasible and infeasible solutions. The penalty-based evaluation function F enriches the objective function with a penalty function DE .

Let $S = \{C_0, C_1, \dots, C_T\}$ be a candidate solution in the enlarged search space, the penalty function $DE(S)$ is defined as the degree of infeasibility of S measured by the total overloaded parts of all the crews to the diversity threshold, i.e., $DE(S) = \sum_{t=1}^T o_t$, where

$$o_t = \begin{cases} D_{min} - D_t, & \text{if } D_t < D_{min} \\ 0, & \text{otherwise} \end{cases} \quad (14)$$

Then the extended evaluation function F is composed of the basic objective function f and penalty function DE :

$$F(S) = f(S) - \beta * DE(S) \quad (15)$$

where $f(S) = \min_{t=\{1, \dots, T\}} \sum_{p \in C_t} e_p$ gives the objective value, $\beta \geq 0$ is a parameter that controls the relative importance given to DE and is dynamically tuned according to a self-adjustment technique [31].

ILS uses the same constrained exchange move defined in Section 5.2, but without any diversity threshold restriction when choosing a candidate solution. To efficiently assess the quality of a candidate solution evaluated by F , the same vectors E , D , and matrix B are maintained in the same manner as FLS. With these data structures, the extended penalty based function value of each neighbor solution S' can be conveniently computed in a similar manner as in FLS in constant time.

ILS is also based on the tabu search framework and is guided by the extended

penalty-based evaluation function F . Algorithm 6 of the Appendix presents the general scheme of the ILS algorithm. At each iteration of ILS, a best admissible candidate solution S' in terms of F is selected to replace the current solution S . During the search process, the value of the self-adjustment parameter β in F is deducted (added) by 1 if all λ consecutive solutions are feasible (infeasible) and its initiating value is set equal to 0. In this work, the value of λ is set to 5 empirically. In general, a small (large) value of β weakly (strongly) penalizes infeasible solutions and leads to the search process to give more importance to infeasible (feasible) solutions. Moreover, the current best feasible solution S^{local_best} is updated by the incumbent solution S if S is a feasible solution and it is better than S^{local_best} in terms of the basic objective value f . The ILS procedure stops after M_{ILS} iterations (M_{ILS} is a parameter), at this point, the FLS procedure is triggered to bring the search back again to the feasible search. Finally, if the solution at the end of the ILS procedure is an infeasible one, the solution repair procedure (Section 5.4) is applied to convert it into a feasible one, which is served as the starting point for the next round of FLS.

5.4 Solution repair procedure

The solution repair procedure is applied to transform an infeasible solution violating the diversity threshold constraint into a feasible one. Specifically, at each step of the solution repair procedure, an individual is selected from the crew C_{min} with the minimum diversity and exchanged with another individual belonging to a different crew C_q satisfying the diversity threshold constraint, such that the diversity of C_{min} increases the most while C_q still complies with the diversity threshold constraint. The above steps are repeated until the solution becomes feasible.

6 Computational experiments

This section is dedicated to a computational assessment of the proposed MA algorithm on a large number of commonly used benchmark instances and comparisons with two heuristic algorithms in the literature: GTS [5] and ABC [9], which are, to our knowledge, the best existing methods for the CMCEE.

6.1 Benchmark instances and experimental protocol

Two sets of benchmark instances were used to test the proposed method. Proposed in [5], the first set (denoted by $I1$, 80 instances) is adapted from the benchmarks originally designed for the Maximum Diversity Problem introduced in [29] with the following characteristics.

- the number of individuals $n = \{100, 200, 300, 400, 500\}$;
- the total number of selected individuals $M = \{10\%, 20\%, 30\%, 40\%\}$ of n ;
- the diversity matrix $DM = d_{pq}$ ($p, q \in \{1, \dots, n\}$) is a real number in the range $[0, 9]$ with uniform distribution.

The CMCEE instances of set $I1$ are then created as follows.

- keep the parameters n and DM unchanged;
- define the quantity of crews T in $\{5, 10\}$;
- define the efficiency vector $EV = e_p$ of the individuals by using random values from an uniform distribution $[1, 100]$;
- define the diversity threshold D_{min} for each crew;
- define M_t by $M_t = \{\frac{0.6*n}{T}, \frac{0.8*n}{T}\}$.

The second set of benchmark instances originates from [9] and includes 240 instances. These instances are generated based on the 80 instances of set $I1$ by using three different diversity thresholds. The diversity thresholds for set $I2$ are set to be a percentage ($\rho \in \{80\%, 100\%, 105\%\}$) of the expected mean diversity of the crews calculated by the following equation [9]:

$$D_{min} = \rho \cdot \frac{(M_t - 1) \cdot M_t \cdot \bar{D}}{2}, \quad \text{with} \quad \bar{D} = \frac{\sum_{p,q \in N} d_{pq}}{n \cdot (n - 1)} \quad (16)$$

Note that a larger ρ generally makes the diversity threshold constraint more difficult to satisfy. The instances in set $I2$ can be divided into three classes according to ρ [9]: easy ($\rho = 80\%$), challenging ($\rho = 100\%$) and difficult ($\rho = 105\%$). All the input data and the detailed numerical results achieved by the proposed algorithm are available at Mendeley’s public repository¹.

The MA algorithm was programmed in C++² and compiled by GNU g++ compiler with the “-O3” option, running on a computer with an Intel Xeon-E5 2695 processor (2.10GHz) and 2GB RAM under Linux operating system. Due to its stochastic nature, the proposed algorithm was ran independently

¹ <https://data.mendeley.com/datasets/zmbnybg9g4/1>

² The source code of our memetic algorithm will be available at: <http://www.info.univ-angers.fr/pub/pub/hao/CMCEE.html>

Table 1
Settings of parameters.

Parameter	Section	Description	Considered values	Final value
$ P $	3.1, 3.2	size of population	{5, 10, 15, 20, 30}	10
β_{max}	5.1	exploration strength of FITS	{5, 10, 15, 20, 30}	15
N_{cons}	5.1, 5.2.2	search depth of each FLS phase	{1000, 2000, 3000, 4000, 5000}	4000
M_{ILS}	5.1, 5.3	maximum number of iterations of each ILS phase	{300, 500, 1000, 2000, 3000}	1000
tt	5.2.2	tabu tenure	{5, 7, 10, 15, 20}	10

30 times on each instance.

6.2 Parameter setting

The MA algorithm requires 5 parameters: population size $|P|$, exploration strength of the FITS algorithm β_{max} , search depth of the FLS phase N_{cons} , maximum number of iterations of the ILS phase M_{ILS} , tabu tenure tt . To identify a proper parameter settings, the popular ‘IRACE’ package for automatic parameter tuning [21] is used on a set of 10 randomly selected instances from set *I1* (02-P100T10M6, 04-P100T5M12, 05-P200T5M24, 10-P300T5M36, 12-P300T10M18, 13-P400T10M24, 15-P400T10M24, 16-P400T5M48, 18-P500T10M30, 19-P500T5M80). For the experiment, the tuning budget was set to 1000 runs, each with a time limit of $n/2$ seconds where n is the number of individuals of the instance. The studied values and final values (suggested by ‘IRACE’) of these parameters are given in Table 1. The same parameter values determined by ‘IRACE’ were used for all experiments conducted in this work.

6.3 Comparative results on the *I1* instances

This section shows a comparison between the proposed MA algorithm and the reference algorithm GTS [5]. In fact, the source codes of the reference algorithms are unavailable and ABC [9] did not report its results on the *I1* instances. To make the comparison as fair as possible, our MA algorithm was ran 30 times on each instance under the same time limit (stopping condition) as in [5] (running Linux on an Intel Core 2 Duo 2.0GHz T7200 processor and 2GB RAM). Table 2 summarizes the comparative results between the two algorithms.

In Table 2, columns 1-2 indicate the instance name (Instance) and the best known results (f_{BK}) [5]. Columns 3-4 present the results obtained by GTS, including the best objective value (f_{best}) and the average computation time

Table 2

Comparative results of the proposed MA algorithm and the GTS algorithm [5] on *I1* instances (part I). The results of the ABC algorithm [9] are unavailable.

Instance	f_{BK}	GTS		MA		
		f_{best}	t_{max}	f_{best}	f_{avg}	t_{avg}
01-P100T10M6	399	399	0.16	420	408.33	0.11
01-P100T10M8	458	458	0.23	501	498.47	0.15
01-P100T5M12	871	871	0.18	846	836.43	0.16
01-P100T5M16	1011	999	0.25	1016	1014.53	0.23
02-P100T10M6	415	398	0.16	429	423.67	0.12
02-P100T10M8	488	469	0.22	504	500.27	0.18
02-P100T5M12	889	889	0.19	876	870.40	0.16
02-P100T5M16	1008	1008	0.24	1016	1015.17	0.23
03-P100T10M6	397	397	0.17	421	411.50	0.12
03-P100T10M8	475	475	0.22	487	470.77	0.21
03-P100T5M12	867	867	0.18	873	862.03	0.18
03-P100T5M16	1002	1002	0.24	1010	1006.97	0.20
04-P100T10M6	409	393	0.15	435	428.20	0.12
04-P100T10M8	490	467	0.22	504	502.53	0.15
04-P100T5M12	863	863	0.17	863	851.50	0.16
04-P100T5M16	990	990	0.24	1010	1007.10	0.21
05-P200T10M12	800	781	0.61	817	812.53	0.50
05-P200T10M16	938	903	0.83	943	941.90	0.56
05-P200T5M24	1645	1645	0.69	1587	1575.63	0.68
05-P200T5M32	1872	1870	0.94	1887	1884.97	0.83
06-P200T10M12	797	781	0.62	817	811.73	0.56
06-P200T10M16	931	905	0.87	942	941.13	0.65
06-P200T5M24	1626	1626	0.67	1638	1629.73	0.58
06-P200T5M32	1876	1864	0.94	1889	1886.63	0.89
07-P200T10M12	788	749	0.61	820	816.40	0.52
07-P200T10M16	936	883	0.91	943	942.67	0.67
07-P200T5M24	1623	1623	0.70	1635	1628.67	0.70
07-P200T5M32	1884	1860	0.93	1890	1889.27	0.82
08-P200T10M16	928	887	0.88	943	940.97	0.70
08-P200T5M24	1641	1641	0.69	1642	1629.70	0.65
08-P200T5M32	1883	1871	0.94	1890	1888.93	0.89
09-P300T10M18	1245	1245	1.38	1269	1260.33	1.34
09-P300T10M24	1468	1440	2.06	1478	1477.57	1.58
09-P300T5M36	2551	2551	1.60	2465	2425.83	1.54
09-P300T5M48	2932	2932	2.12	2954	2950.57	2.08
10-P300T10M18	1233	1233	1.39	1258	1238.10	1.35
10-P300T10M24	1434	1433	2.26	1472	1466.73	1.92
10-P300T5M36	2559	2559	1.87	2486	2464.07	1.81
10-P300T5M48	2947	2938	2.63	2953	2950.70	2.59
11-P300T10M18	1265	1265	1.78	1276	1269.33	1.28
11-P300T10M24	1471	1455	2.32	1478	1476.43	1.69

Table 2

Comparative results of the proposed MA algorithm and the GTS algorithm [5] on *I1* instances (part II). The results of the ABC algorithm [9] are unavailable.

Instance	f_{BK}	GTS		MA		
		f_{best}	t_{max}	f_{best}	f_{avg}	t_{avg}
11-P300T5M36	2556	2556	1.93	2570	2559.33	1.86
11-P300T5M48	2957	2937	2.67	2959	2959.00	0.84
12-P300T10M18	1242	1242	1.68	1273	1265.57	1.36
12-P300T10M24	1469	1438	2.32	1478	1477.17	1.55
12-P300T5M36	2542	2542	1.90	2505	2479.17	1.84
12-P300T5M48	2955	2921	2.62	2959	2957.50	2.39
13-P400T10M24	1707	1707	3.09	1707	1626.33	2.69
13-P400T10M32	1998	1979	5.02	2011	2009.07	3.10
13-P400T5M48	3471	3471	3.28	3414	3399.43	3.08
13-P400T5M64	4004	4000	4.81	4023	4019.90	4.73
14-P400T10M24	1697	1697	2.93	1723	1712.70	2.77
14-P400T10M32	2000	1961	4.40	2012	2009.30	3.49
14-P400T5M48	3466	3466	3.52	3329	3278.60	3.38
14-P400T5M64	4008	3998	4.81	4025	4022.13	4.49
15-P400T10M24	1702	1702	3.02	1709	1703.70	2.39
15-P400T10M32	1999	1974	4.24	2011	2009.67	3.83
15-P400T5M48	3473	3473	3.48	3414	3387.80	3.25
15-P400T5M64	4018	4001	4.71	4026	4025.23	4.66
16-P400T10M24	1685	1685	2.94	1713	1697.33	2.30
16-P400T10M32	1989	1952	4.36	2010	2007.47	3.84
16-P400T5M48	3470	3470	3.66	3428	3400.10	3.57
16-P400T5M64	4024	3993	4.62	4026	4025.33	3.93
17-P500T10M30	2145	2145	5.39	2145	2070.30	4.00
17-P500T10M40	2483	2483	6.67	2501	2496.27	5.95
17-P500T5M60	4332	4332	5.64	4082	4023.37	5.58
17-P500T5M80	4989	4989	7.58	4992	4975.80	7.24
18-P500T10M30	2132	2132	5.03	2135	2082.10	4.20
18-P500T10M40	2486	2461	6.75	2505	2502.10	6.17
18-P500T5M60	4354	4354	5.64	4109	4045.40	5.51
18-P500T5M80	5000	5000	7.54	5008	5001.57	7.47
19-P500T10M30	2133	2133	5.44	2141	2072.17	4.03
19-P500T10M40	2470	2470	6.95	2497	2489.43	6.54
19-P500T5M60	4335	4335	5.58	4199	4165.47	5.55
19-P500T5M80	4987	4987	7.58	5006	4992.57	7.38
20-P500T10M30	2131	2114	4.96	2179	2165.73	4.49
20-P500T10M40	2504	2446	6.56	2509	2508.23	4.17
20-P500T5M60	4346	4346	5.51	4217	4179.47	5.33
20-P500T5M80	4995	4995	7.40	5009	5002.37	7.29
#Improve		0		63		
#Match		17		3		
#Total		80		80		
<i>p</i> -value		1.59e-3				

(t_{max}) in seconds to complete its execution. The results of GTS are directly taken from [5]. The last three columns report the results produced by our MA algorithm, including the best objective value (f_{best}), the average objective value (f_{avg}) and average run time (t_{avg}) in seconds to reach the best objective value. Rows ‘#Improve’ and ‘#Match’ report respectively the number of cases for which each algorithm improves or matches the best-known results from the literature. Row ‘#Total’ denotes the total number of instances. Row p -value indicates the results from the Wilcoxon signed-rank test with a confidence level of 95% between the compared algorithms. The results in bold are the best results among f_{BK} and f_{best} of the compared algorithms.

The comparison mainly focuses on solution quality in terms of the objective values, while the timing information is provided only for indicative purposes. Since the two compared algorithms were run on different computing platforms, the Standard Performance Evaluation Cooperation tool (www.spec.org) is used to obtain the scale ratio ($2.10/2.00 = 1.05$) of the CPU frequencies, which indicates that our computer is slightly (1.05 time) faster.

Table 2 indicates that MA performs better than GTS by finding 63 improved lower bounds and matching the best known results on 3 cases while MA is outperformed by GTS for the remaining 14 instances. The Wilcoxon signed-rank test (p -value < 0.05) also confirms the dominance of MA over GTS. This experiment shows that MA is highly efficient for the $I1$ instances compared to the GTS algorithm.

6.4 Comparative results on the $I2$ instances

To further assess the performance of our MA algorithm, this section compares MA with the two reference algorithms GTS [5] and ABC [9] on the $I2$ instances. A summary of the comparative results is shown in Table 3. Row ‘#Best’ denotes the number of instances for which the corresponding algorithm produces the best result among all the compared algorithms. The last row gives the p -values from the Wilcoxon signed-rank test with a confidence level of 95%. The symbol ‘-’ indicates that the corresponding algorithm cannot obtain a feasible solution on the instance within the time limit with $n/2$ seconds and other symbols have the same meanings as those in Table 2. The results for GTS and ABC are directly compiled from [9] and were obtained on a platform equipped with an Intel i5 quad-core processor (2.90GHz) and 8 GB RAM running on MAC OS X operating system. Note that the results on the $I2$ instances reported for GTS were based on the implementation by the authors of [9]. The scale ratio ($2.10/2.90 \approx 0.72$) of the CPU frequencies from SPEC (www.spec.org) indicates that our computer is slower than the computer used in [9].

Table 3. Comparative results of the proposed MA algorithm and the reference algorithms (ABC [9] and GTS [5]) on $I2$ instances (part I).

Instance	$\rho = 80\%$						$\rho = 100\%$						$\rho = 105\%$					
	ABC		GTS		MA		ABC		GTS		MA		ABC		GTS		MA	
	f_{best}	t_{avg}	f_{best}	t_{avg}	f_{avg}	t_{avg}	f_{best}	t_{avg}	f_{best}	t_{avg}	f_{avg}	t_{avg}	f_{best}	t_{avg}	f_{best}	t_{avg}	f_{avg}	t_{avg}
01-P100T10M6	301	243	449	449.00	0.04	0.06	-	243	449	449.00	0.06	-	449	449.00	0.04	0.06	449.00	0.04
01-P100T10M8	401	406	508	508.00	0.01	0.03	-	421	508	508.00	0.03	-	508	508.00	0.06	0.06	508.00	0.06
01-P100T5M12	704	654	899	899.00	0.03	0.05	690	538	899	899.00	0.05	926	899.00	0.06	0.06	899.00	0.06	
01-P100T5M16	896	802	1016	1016.00	0.09	0.13	903	837	1016	1016.00	0.13	926	1016.00	0.15	0.15	1016.00	0.15	
02-P100T10M6	319	292	449	449.00	0.05	0.07	323	347	449	449.00	0.07	-	449	449.00	0.08	0.08	449.00	0.08
02-P100T10M8	418	412	508	508.00	0.04	0.05	406	430	508	508.00	0.05	-	508	508.00	0.06	0.06	508.00	0.06
02-P100T5M12	733	665	899	899.00	0.03	0.03	737	680	899	899.00	0.03	704	899.00	0.04	0.04	899.00	0.04	
02-P100T5M16	932	881	1016	1016.00	0.02	0.02	915	856	1016	1016.00	0.03	902	1016.00	0.03	0.03	1016.00	0.03	
03-P100T10M6	308	333	449	449.00	0.06	0.06	-	160	449	449.00	0.05	-	449	449.00	0.06	0.06	449.00	0.06
03-P100T10M8	416	438	508	508.00	0.07	0.07	397	246	508	508.00	0.07	-	508	508.00	0.09	0.09	508.00	0.09
03-P100T5M12	736	719	899	899.00	0.30	0.30	732	682	899	899.00	0.47	-	899	899.00	0.51	0.51	899.00	0.51
03-P100T5M16	919	861	1016	1016.00	0.06	0.06	947	835	1016	1016.00	0.06	-	1016	1016.00	0.08	0.08	1016.00	0.08
04-P100T10M6	316	314	449	449.00	0.04	0.04	-	-	449	449.00	0.07	-	449	449.00	0.10	0.10	449.00	0.10
04-P100T10M8	417	387	508	508.00	0.05	0.05	416	-	508	508.00	0.12	401	508.00	0.15	0.15	508.00	0.15	
04-P100T5M12	718	648	899	899.00	0.15	0.15	731	674	899	899.00	0.10	-	899	899.00	0.18	0.18	899.00	0.18
04-P100T5M16	915	879	1016	1016.00	0.02	0.02	915	871	1016	1016.00	0.04	-	1016	1016.00	0.02	0.02	1016.00	0.02
05-P200T10M12	584	550	833	833.00	0.30	0.30	589	594	833	833.00	0.36	-	833	833.00	0.50	0.50	833.00	0.50
05-P200T10M16	768	742	945	945.00	0.28	0.28	767	705	945	945.00	0.29	-	945	945.00	0.34	0.34	945.00	0.34
05-P200T5M24	1294	1171	1667	1667.00	0.18	0.18	1279	1190	1667	1667.00	0.33	-	1667	1667.00	0.73	0.73	1667.00	0.73
05-P200T5M32	1651	1553	1890	1890.00	0.20	0.20	1661	1499	1890	1890.00	0.20	-	1890	1890.00	0.26	0.26	1890.00	0.26
06-P200T10M12	600	585	833	833.00	0.22	0.22	586	597	833	833.00	0.23	-	833	833.00	0.33	0.33	833.00	0.33
06-P200T10M16	774	781	945	945.00	0.31	0.31	760	777	945	945.00	0.34	-	945	945.00	0.47	0.47	945.00	0.47
06-P200T5M24	1316	1187	1667	1667.00	0.64	0.64	1323	1204	1667	1667.00	0.89	-	1667	1667.00	1.04	1.04	1667.00	1.04
06-P200T5M32	1669	1615	1890	1890.00	2.67	2.67	1677	1626	1890	1890.00	3.13	-	1890	1890.00	3.51	3.51	1890.00	3.51
07-P200T10M12	568	525	833	833.00	0.20	0.20	574	550	833	833.00	0.25	-	833	833.00	0.29	0.29	833.00	0.29
07-P200T10M16	753	724	945	945.00	0.21	0.21	760	799	945	945.00	0.32	-	945	945.00	0.43	0.43	945.00	0.43
07-P200T5M24	1299	1249	1667	1667.00	0.70	0.70	1344	1315	1667	1667.00	1.35	-	1667	1667.00	1.73	1.73	1667.00	1.73
07-P200T5M32	1684	1624	1890	1890.00	0.34	0.34	1688	-	1890	1890.00	0.75	-	1890	1890.00	0.78	0.78	1890.00	0.78
08-P200T10M12	593	477	833	833.00	0.21	0.21	-	558	833	833.00	0.24	-	833	833.00	0.36	0.36	833.00	0.36
08-P200T10M16	791	704	945	945.00	0.34	0.34	784	714	945	945.00	0.32	-	945	945.00	0.38	0.38	945.00	0.38
08-P200T5M24	1320	1166	1667	1667.00	1.26	1.26	1310	1221	1667	1667.00	1.96	-	1667	1667.00	2.30	2.30	1667.00	2.30
08-P200T5M32	1687	1613	1890	1890.00	0.18	0.18	1665	1571	1890	1890.00	0.20	-	1890	1890.00	0.34	0.34	1890.00	0.34
09-P300T10M18	914	820	1294	1294.00	0.41	0.41	900	857	1294	1294.00	0.55	-	1294	1294.00	0.84	0.84	1294.00	0.84
09-P300T10M24	1192	1147	1479	1479.00	0.77	0.77	1194	1083	1479	1479.00	0.79	-	1479	1479.00	0.82	0.82	1479.00	0.82
09-P300T5M36	2005	1890	2589	2589.00	1.37	1.37	2011	1958	2589	2589.00	1.89	-	2589	2589.00	2.96	2.96	2589.00	2.96
09-P300T5M48	2580	2479	2959	2959.00	0.45	0.45	2529	2563	2959	2959.00	0.42	-	2959	2959.00	1.13	1.13	2959.00	1.13
10-P300T10M18	882	875	1294	1294.00	0.67	0.67	865	-	1294	1294.00	0.47	-	1294	1294.00	0.77	0.77	1294.00	0.77
10-P300T10M24	1164	1171	1479	1479.00	0.74	0.74	1204	-	1479	1479.00	0.82	-	1479	1479.00	0.61	0.61	1479.00	0.61
10-P300T5M36	1958	1820	2589	2589.00	0.42	0.42	1955	1808	2589	2589.00	0.46	-	2589	2589.00	0.47	0.47	2589.00	0.47
10-P300T5M48	2583	2412	2959	2959.00	0.44	0.44	2585	2430	2959	2959.00	0.48	-	2959	2959.00	0.39	0.39	2959.00	0.39
11-P300T10M18	914	939	1294	1294.00	0.57	0.57	899	896	1294	1294.00	0.62	-	1294	1294.00	1.14	1.14	1294.00	1.14
11-P300T10M24	1209	1213	1479	1479.00	0.72	0.72	1195	-	1479	1479.00	0.71	-	1479	1479.00	0.66	0.66	1479.00	0.66

Table 3. Comparative results of the proposed MA algorithm and the reference algorithms (ABC [9] and GTS [5]) on $I2$ instances (part II).

Instance	$\rho = 80\%$						$\rho = 100\%$						$\rho = 105\%$					
	ABC		GTS		MA		ABC		GTS		MA		ABC		GTS		MA	
	f_{best}	t_{avg}	f_{best}	t_{avg}	f_{avg}	t_{avg}	f_{best}	t_{avg}	f_{best}	t_{avg}	f_{avg}	t_{avg}	f_{best}	t_{avg}	f_{best}	t_{avg}	f_{avg}	t_{avg}
11-P300T5M36	2046	1856	2589	2589.00	2.85	2006	1712	2589	2589.00	3.09	-	2589	2589.00	3.50				
11-P300T5M48	2644	2351	2959	2959.00	2.09	2522	2412	2959	2959.00	2.31	-	2959	2959.00	3.47				
12-P300T10M18	948	783	1294	1294.00	0.50	899	791	1294	1294.00	0.58	-	1294	1294.00	0.46				
12-P300T10M24	1200	1126	1479	1479.00	0.79	1197	1165	1479	1479.00	0.92	-	1479	1479.00	0.61				
12-P300T5M36	1951	1937	2589	2589.00	1.89	2010	1778	2589	2589.00	1.93	-	2589	2589.00	2.71				
12-P300T5M48	2621	2398	2959	2959.00	1.47	2572	2525	2959	2959.00	1.87	-	2959	2959.00	3.28				
13-P400T10M24	1233	1174	1754	1754.00	1.09	-	-	1754	1754.00	1.18	-	1754	1754.00	1.24				
13-P400T10M32	1645	1602	2013	2013.00	1.99	-	1694	2013	2013.00	2.20	-	2013	2013.00	2.52				
13-P400T5M48	2715	2324	3509	3509.00	2.65	2702	2526	3509	3509.00	4.08	-	3509	3509.00	4.67				
13-P400T5M64	3521	3314	4026	4026.00	1.60	3550	3339	4026	4026.00	1.87	-	4026	4026.00	2.30				
14-P400T10M24	1228	1118	1754	1754.00	1.04	1229	1168	1754	1754.00	1.11	-	1754	1754.00	1.04				
14-P400T10M32	1634	1581	2013	2013.00	1.84	1658	1466	2013	2013.00	2.24	-	2013	2013.00	2.45				
14-P400T5M48	2666	2420	3509	3509.00	5.92	2666	2437	3509	3509.00	7.66	-	3509	3509.00	9.04				
14-P400T5M64	3506	3268	4026	4026.00	1.33	3523	3143	4026	4026.00	0.96	-	4026	4026.00	1.64				
15-P400T10M24	1271	1238	1754	1754.00	1.07	1241	1322	1754	1754.00	1.21	-	1754	1754.00	1.69				
15-P400T10M32	1651	1632	2013	2013.00	1.78	1657	1662	2013	2013.00	2.53	-	2013	2013.00	2.89				
15-P400T5M48	2720	2482	3509	3509.00	2.82	2668	2535	3509	3509.00	4.28	-	3509	3509.00	4.83				
15-P400T5M64	3563	3307	4026	4026.00	1.57	3562	3238	4026	4026.00	2.25	-	4026	4026.00	3.13				
16-P400T10M24	1265	1156	1754	1754.00	1.03	-	-	1754	1754.00	1.43	-	1754	1754.00	1.96				
16-P400T10M32	1637	1597	2013	2013.00	1.86	-	-	2013	2013.00	2.30	-	2013	2013.00	2.70				
16-P400T5M48	2708	2538	3509	3509.00	1.78	2784	2557	3509	3509.00	1.96	-	3509	3509.00	2.63				
16-P400T5M64	3472	3278	4026	4026.00	0.86	3459	3427	4026	4026.00	1.13	-	4026	4026.00	3.72				
17-P500T10M30	1530	1537	2189	2189.00	1.73	1507	1554	2189	2189.00	2.02	-	2189	2189.00	2.97				
17-P500T10M40	2037	1972	2509	2508.20	2.10	-	2065	2509	2509.00	2.76	-	2509	2509.00	3.89				
17-P500T5M60	3233	3200	4378	4378.00	4.13	3289	-	4378	4378.00	5.71	-	4378	4378.00	6.43				
17-P500T5M80	4289	4250	5019	5019.00	1.97	4266	-	5019	5019.00	2.41	-	5019	5019.00	3.63				
18-P500T10M30	1574	1526	2189	2189.00	2.17	-	1663	2189	2189.00	3.08	-	2189	2189.00	3.77				
18-P500T10M40	2067	1982	2509	2506.70	2.78	-	2107	2509	2509.00	4.24	-	2509	2509.00	5.14				
18-P500T5M60	3392	2836	4378	4378.00	1.79	3326	3081	4378	4378.00	1.81	-	4378	4378.00	3.06				
18-P500T5M80	4349	3960	5019	5019.00	0.90	4355	4072	5019	5019.00	2.12	-	5019	5019.00	4.20				
19-P500T10M30	1535	1455	2189	2189.00	2.87	1528	1446	2189	2189.00	5.08	-	2189	2189.00	5.37				
19-P500T10M40	2031	1906	2509	2508.27	4.49	-	2011	2509	2509.00	6.62	-	2509	2509.00	8.83				
19-P500T5M60	3288	3107	4378	4378.00	4.68	3304	3247	4378	4378.00	5.26	-	4378	4378.00	5.41				
19-P500T5M80	4325	4144	5019	5019.00	0.50	4391	4243	5019	5019.00	1.88	-	5019	5019.00	5.56				
20-P500T10M30	1551	1481	2189	2189.00	2.78	1543	1535	2189	2189.00	4.35	-	2189	2189.00	5.20				
20-P500T10M40	2023	2002	2509	2507.17	2.18	2026	2069	2509	2509.00	6.87	-	2509	2509.00	8.28				
20-P500T5M60	3339	3289	4378	4378.00	0.88	3408	3236	4378	4378.00	1.20	-	4378	4378.00	2.63				
20-P500T5M80	4305	4216	5019	5019.00	0.59	4358	4363	5019	5019.00	2.00	-	5019	5019.00	6.61				
#Best	0	0	80	80	80	0	0	80	80	80	0	0	80	80				
p-value	7.85e-15	7.84e-15	7.84e-15	7.85e-15	7.84e-15	7.84e-15	7.85e-15	7.84e-15	7.85e-15	7.84e-15	7.73e-15	7.71e-15	7.73e-15	7.71e-15				

Table 4

Comparison results between FITS, FLS and ILS on the 10 randomly selected instances of $I1$ set.

Instance	FITS			FLS			ILS		
	f_{best}	f_{avg}	t_{avg}	f_{best}	f_{avg}	t_{avg}	f_{best}	f_{avg}	t_{avg}
02-P100T10M6	435	424.27	0.12	431	405.23	0.03	420	362.77	0.12
04-P100T5M12	863	849.40	0.16	857	839.97	0.12	859	794.07	0.13
05-P200T5M24	1591	1575.50	0.68	1586	1572.43	0.63	1563	1372.83	0.62
10-P300T5M36	2492	2470.83	1.75	2488	2467.80	1.52	2425	2275.53	1.27
12-P300T10M18	1279	1273.50	1.44	1276	1171.50	0.75	1246	1138.47	1.27
13-P400T10M24	1707	1640.40	2.73	1677	1442.20	1.10	1456	1325.40	1.91
15-P400T10M24	1726	1708.77	2.82	1717	1663.80	1.65	1622	1475.27	1.87
16-P400T5M48	3439	3413.33	3.52	3435	3404.10	3.38	3348	3050.07	3.37
18-P500T10M30	2135	2096.73	4.69	2120	1997.20	2.79	1975	1752.27	3.54
19-P500T5M80	5011	4998.87	7.33	5008	4996.10	6.96	4949	4762.20	4.82
#Best	10	10		0	0		0	0	
$Avg_t(s)$			2.52			1.89			1.89

One observes from Table 3 that our MA algorithm outperforms these two reference algorithms on the $I2$ set by producing the best result for all 240 instances in terms of the best objective value. One also notices that, for all 240 instances, even our *average* results (f_{avg}) across the 30 independent runs are better than the *best* results of the two reference algorithms. Furthermore, the superiority of MA over each reference algorithm is confirmed by the Wilcoxon signed-rank test with p -values less than 0.05. This experiment demonstrates that MA competes very favorably with the reference algorithms on this set of instances.

7 Analysis

This section is dedicated to an analysis of several key ingredients of the proposed algorithm to illustrate their influences on the performance of the algorithm, which includes the combined use of feasible and infeasible local searches, the motivation behind the backbone-based crossover and the effect of the memetic framework. The experiments were conducted on 10 randomly selected instances from the $I1$ set and 30 instances from the $I2$ set, covering three different diversity thresholds $\rho = 80\%$, $\rho = 100\%$ and $\rho = 105\%$.

Table 5

Comparison results between FITS, FLS and ILS on 30 instances of $I2$ set with different thresholds $\rho = 80\%$, $\rho = 100\%$ and $\rho = 105\%$.

ρ	Instance	FITS			FLS			ILS		
		f_{best}	f_{avg}	t_{avg}	f_{best}	f_{avg}	t_{avg}	f_{best}	f_{avg}	t_{avg}
80%										
	02-P100T10M6	449	449.00	0.03	449	449.00	0.01	449	449.00	0.01
	04-P100T5M12	899	898.93	0.28	899	898.87	0.06	899	898.70	0.01
	05-P200T5M24	1667	1666.97	0.13	1667	1666.97	0.05	1667	1666.93	0.04
	10-P300T5M36	2589	2589.00	0.30	2589	2588.97	0.25	2589	2588.93	0.26
	12-P300T10M18	1294	1293.97	0.29	1294	1293.97	0.13	1294	1293.97	0.11
	13-P400T10M24	1754	1754.00	0.87	1754	1754.00	0.68	1754	1754.00	0.65
	15-P400T10M24	1754	1753.97	0.93	1754	1753.97	1.04	1754	1753.93	0.74
	16-P400T5M48	3509	3508.43	0.89	3509	3508.23	0.68	3509	3508.33	0.67
	18-P500T10M30	2189	2188.80	1.20	2189	2188.80	2.15	2189	2188.33	0.36
	19-P500T5M80	5019	5018.70	0.33	5019	5018.67	0.75	5019	5018.07	0.25
100%										
	02-P100T10M6	449	449.00	0.06	449	449.00	0.03	449	449.00	0.02
	04-P100T5M12	899	899.00	0.05	899	899.00	0.03	899	899.00	0.02
	05-P200T5M24	1667	1666.93	0.12	1667	1666.90	0.12	1667	1666.87	0.10
	10-P300T5M36	2589	2589.00	0.35	2589	2589.00	0.32	2589	2589.00	0.33
	12-P300T10M18	1294	1293.93	0.38	1294	1293.90	0.29	1294	1293.17	0.25
	13-P400T10M24	1754	1754.00	0.98	1754	1754.00	0.76	1754	1754.00	0.69
	15-P400T10M24	1754	1753.97	1.03	1754	1753.97	0.93	1754	1753.97	0.76
	16-P400T5M48	3509	3508.60	1.21	3509	3508.33	0.76	3509	3508.53	0.74
	18-P500T10M30	2189	2189.00	2.11	2189	2189.00	2.15	2189	2189.00	0.69
	19-P500T5M80	5019	5018.70	1.02	5019	5018.67	0.93	5019	5018.67	0.47
105%										
	02-P100T10M6	449	449.00	0.06	449	449.00	0.04	449	449.00	0.02
	04-P100T5M12	899	899.00	0.16	899	899.00	0.06	899	899.00	0.07
	05-P200T5M24	1667	1667.00	0.58	1667	1666.83	0.24	1667	1666.47	0.16
	10-P300T5M36	2589	2589.00	0.43	2589	2588.97	0.36	2589	2589.00	0.38
	12-P300T10M18	1294	1294.00	0.39	1294	1294.00	0.31	1294	1293.93	0.28
	13-P400T10M24	1754	1754.00	1.02	1754	1754.00	0.84	1754	1754.00	0.81
	15-P400T10M24	1754	1753.93	1.28	1754	1753.83	1.03	1754	1753.67	0.87
	16-P400T5M48	3509	3508.70	2.12	3509	3508.67	0.89	3509	3508.60	1.04
	18-P500T10M30	2189	2188.97	2.78	2189	2188.90	2.34	2189	2188.83	1.46
	19-P500T5M80	5019	5017.33	3.56	5019	5017.23	3.38	5019	5017.13	1.26
#Best		30	30		30	17		30	14	
$Avg_t(s)$				0.83			0.72			0.45

7.1 Effect of the combined use of feasible and infeasible local searches

A key feature of FITS is the hybrid scheme integrating both feasible and infeasible local search methods. To examine the merit of the hybrid scheme, an experiment was conducted to compare FITS and its two underlying local search (FLS and ILS) procedures.

The comparative results are summarized in Tables 4 and 5. The average run time in seconds to reach the best objective value for all the test instances is given in the last row (Avg_t). Tables 4 and 5 show that FITS produced the best result on all 40 instances in terms of the best objective value whereas FLS

Table 6

Percentage of individuals in the same crews in local optima of different qualities on a random selection of 10 instances from *I1* set.

Instance	S_{hq}	S_{all}	S_{lo}	Instance	S_{hq}	S_{all}	S_{lo}
02-P100T10M6	0.84	0.71	0.55	13-P400T10M24	0.92	0.64	0.29
04-P100T5M12	0.86	0.69	0.57	15-P400T10M24	0.85	0.63	0.35
05-P200T5M24	0.81	0.64	0.35	16-P400T5M48	0.87	0.68	0.43
10-P300T5M36	0.79	0.58	0.41	18-P500T10M30	0.82	0.59	0.25
12-P300T10M18	0.76	0.57	0.38	19-P500T5M80	0.83	0.63	0.40

Table 7

Percentage of individuals in the same crews in local optima of different qualities on 30 instances from *I2* set with different diversity thresholds ρ .

Instance	$\rho = 80\%$			$\rho = 100\%$			$\rho = 105\%$		
	S_{hq}	S_{all}	S_{lo}	S_{hq}	S_{all}	S_{lo}	S_{hq}	S_{all}	S_{lo}
02-P100T10M6	0.84	0.70	0.46	0.72	0.50	0.35	0.78	0.59	0.46
04-P100T5M12	0.64	0.46	0.35	0.81	0.58	0.44	0.89	0.62	0.50
05-P200T5M24	0.87	0.68	0.48	0.76	0.61	0.48	0.94	0.70	0.49
10-P300T5M36	0.85	0.57	0.36	0.74	0.50	0.35	0.95	0.76	0.53
12-P300T10M18	0.64	0.49	0.31	0.81	0.66	0.46	0.94	0.69	0.51
13-P400T10M24	0.89	0.69	0.45	0.90	0.65	0.42	0.77	0.65	0.40
15-P400T10M24	0.87	0.66	0.43	0.89	0.58	0.36	0.85	0.58	0.42
16-P400T5M48	0.67	0.49	0.32	0.84	0.63	0.45	0.91	0.67	0.41
18-P500T10M30	0.80	0.60	0.38	0.87	0.67	0.52	0.88	0.64	0.37
19-P500T5M80	0.69	0.47	0.29	0.89	0.62	0.51	0.81	0.58	0.34

and ILS yielded the best result on 30, 30 cases respectively. When comparing the average objective value over 30 independent runs, FITS obtained the best result on all the instances, while FLS and ILS produced the best result on 17, 14 out of the 40 instances respectively. The Wilcoxon signed-rank test leads to small p -values in terms of the best solution values (average solution values): $4.92e-3$ ($1.81e-5$) for FITS v.s. FLS, and $5.06e-3$ ($5.60e-6$) for FITS v.s. ILS. This experiment demonstrates the effectiveness of the hybrid scheme integrating both the feasible and infeasible local searches.

7.2 Motivation behind the backbone-based crossover

To explain the use of the proposed backbone-based crossover, this section investigates the structural similarity between local optima having different qualities. Given two local optima S^1 and S^2 , the similarity between them is defined as the percentage of individuals grouped together in both S^1 and S^2 : $sim(S^1, S^2) = \frac{|J|}{n}$ where J denotes the set of individuals grouped together in S^1 and S^2 . J is identified by using the group matching algorithm proposed in Section 4.

Table 8

Comparison results between FITS and MA on the 10 randomly selected instances of $I1$ set.

Instance	FITS			MA		
	f_{best}	f_{avg}	t_{avg}	f_{best}	f_{avg}	t_{avg}
02-P100T10M6	435	428.83	0.88	435	429.17	1.17
04-P100T5M12	863	858.13	1.02	863	858.97	1.42
05-P200T5M24	1591	1585.97	5.24	1591	1586.63	6.61
10-P300T5M36	2499	2491.93	15.34	2505	2493.77	17.08
12-P300T10M18	1281	1278.70	8.73	1283	1279.90	12.09
13-P400T10M24	1707	1661.97	17.52	1707	1678.13	18.57
15-P400T10M24	1729	1722.93	19.32	1729	1724.20	19.45
16-P400T5M48	3445	3433.93	31.16	3446	3437.83	30.39
18-P500T10M30	2147	2118.33	29.13	2151	2129.17	30.01
19-P500T5M80	5011	5009.53	71.33	5013	5009.97	73.90
#Best	5	0		10	10	
$Avg_t(s)$			19.97			21.07

For this analysis, the same 40 instances (10 $I1$ instances and 30 $I2$ instances) as before were used. For each instance, 1000 local optima of different qualities were produced by using FITS and MA. Then the top 10% (100) local optima having the largest objective values are selected to form the set of ‘high-quality solutions’, and the bottom 10% (100) solutions with the smallest objective values are used to build the set of ‘low-quality solutions’.

Tables 6 and 7 show the experimental results. Columns S_{hq} , S_{all} and S_{lo} represent respectively the percentage of common individuals grouped across the set of 100 high-quality solutions, the set of 1000 sampled local optima and the set of 100 low-quality solutions. It is observed that the percentage of individuals grouped together across the solutions from the set of high-quality solutions is large, ranging from 0.64 to 0.95. This observation provides the basis for the proposed backbone crossover operator, which preserves the common individuals grouped together between two parent solutions.

7.3 Usefulness of the memetic framework

To analyze the effect of the memetic framework, the MA algorithm was compared with a multi-start version of the FITS algorithm. For this experiment, both FITS and MA were executed independently 30 times on each instance with a time limit of $n/2$ seconds per run. Notice that the FITS algorithm was run in a multi-start way by generating a random initial solution for each restart until the cutoff time was reached.

Table 9

Comparisons between FITS and MA on 30 instances of $I2$ set with different thresholds $\rho = 80\%$, $\rho = 100\%$ and $\rho = 105\%$.

ρ	Instance	FITS			MA		
		f_{best}	f_{avg}	t_{avg}	f_{best}	f_{avg}	t_{avg}
80%							
	02-P100T10M6	449	449.00	0.03	449	449.00	0.05
	04-P100T5M12	899	898.83	0.13	899	899.00	0.15
	05-P200T5M24	1667	1666.87	0.11	1667	1667.00	0.18
	10-P300T5M36	2589	2589.00	0.32	2589	2589.00	0.42
	12-P300T10M18	1294	1293.67	0.26	1294	1294.00	0.50
	13-P400T10M24	1754	1754.00	0.82	1754	1754.00	1.09
	15-P400T10M24	1754	1753.87	0.83	1754	1754.00	1.07
	16-P400T5M48	3509	3508.63	0.98	3509	3509.00	1.78
	18-P500T10M30	2189	2188.87	1.40	2189	2189.00	2.87
	19-P500T5M80	5019	5018.73	0.36	5019	5019.00	0.50
100%							
	02-P100T10M6	449	449.00	0.05	449	449.00	0.07
	04-P100T5M12	899	899.00	0.06	899	899.00	0.10
	05-P200T5M24	1667	1666.97	0.18	1667	1667.00	0.33
	10-P300T5M36	2589	2589.00	0.41	2589	2589.00	0.46
	12-P300T10M18	1294	1293.83	0.31	1294	1294.00	0.58
	13-P400T10M24	1754	1754.00	0.93	1754	1754.00	1.18
	15-P400T10M24	1754	1753.97	1.07	1754	1754.00	1.21
	16-P400T5M48	3509	3508.33	1.06	3509	3509.00	1.96
	18-P500T10M30	2189	2189.00	1.97	2189	2189.00	3.08
	19-P500T5M80	5019	5018.87	1.31	5019	5019.00	1.88
105%							
	02-P100T10M6	449	449.00	0.06	449	449.00	0.08
	04-P100T5M12	899	899.00	0.14	899	899.00	0.18
	05-P200T5M24	1667	1667.00	0.63	1667	1667.00	0.73
	10-P300T5M36	2589	2589.00	0.44	2589	2589.00	0.47
	12-P300T10M18	1294	1294.00	0.41	1294	1294.00	0.46
	13-P400T10M24	1754	1754.00	1.12	1754	1754.00	1.24
	15-P400T10M24	1754	1753.97	1.38	1754	1754.00	1.69
	16-P400T5M48	3509	3508.87	2.34	3509	3509.00	2.63
	18-P500T10M30	2189	2189	3.18	2189	2189.00	3.77
	19-P500T5M80	5019	5018.83	4.56	5019	5019.00	5.56
#Best		30	15		30	30	
$Avg_t(s)$				0.89			1.21

Tables 8 and 9 summarize the computational results of the compared algorithms. One observes that MA performs better than FITS in terms of both the best and the average objective values. Specifically, MA obtained the best result on all 40 instances considering the best objective value, whereas

FITS yielded the best result on 35 out of 40 instances. In terms of the average objective value, MA produced the best result on all the 40 instances, while FITS only obtained the best result on 15 instances. The average computation time to reach the best objective value for all 40 instances indicates that MA is a little slower than FITS. The Wilcoxon signed-rank test (p -value of $4.22e - 2$ and $1.20e - 5$ in terms of best and average results) supports the superiority of MA over FITS.

8 Conclusions

This work introduced the first population-based memetic algorithm for solving the problem of composing medical crews with equity and efficiency. The proposed algorithm combines a backbone-based crossover for generating new promising solutions and a powerful local optimization procedure mixing feasible search and infeasible search to ensure an effective examination of the search space. The computational experiments demonstrated that our algorithm dominates the best performing approaches in the literature. Specifically, it discovers improved best solutions (new lower bounds) for 303 out of the 320 test instances ($\approx 95\%$). This work thus advances the state of the art for solving the benchmark instances of the problem. More importantly, the publicly available code of our algorithm can be freely used by researchers and practitioners in health care service management (e.g., to compose medical crews with a high equity and efficiency) and could incite more research on this important application as well.

Meanwhile, given that the proposed algorithm is a heuristic method, one does not know how far the reported solutions are from the optimal solutions. As a result, more research is needed to investigate exact and approximation approaches with quality guarantee. Moreover, to further improve the search capacity of the proposed algorithm, it would be interesting to investigate machine learning techniques [6,20,28,32] to make the search process more effective. In addition, the studied problem requires the simultaneous consideration of two conflicting criteria (equity and efficiency). It is thus a special case of the general multi-objective optimization. Consequently, it would be interesting to investigate popular evolutionary multi-objective optimization approach, in particular scalable algorithms [15] to deal with large-scale problems in modern medical service systems. Finally, the search strategies of the proposed algorithm follow general principles and could be applied to design algorithms for other problems with equity and efficiency requirements.

Acknowledgment

We are grateful to the reviewers for their useful comments and suggestions which helped us to significantly improve the paper.

References

- [1] Aboueljinane, L., Sahin, E., & Jemai, Z. (2013). A review on simulation models applied to emergency medical service operations. *Computers & Industrial Engineering*, 66(4), 734-750.
- [2] Abualigah, L., Alfar, H. E., Shehab, M., & Hussein, A. M. A. (2020). Sentiment Analysis in Healthcare: A Brief Review. In: Abd Elaziz M., Al-qaness M., Ewees A., & Dahou A. (Eds.), *Recent Advances in NLP: The Case of Arabic Language*, Studies in Computational Intelligence, Vol 874 (pp. 129-141). Cham: Springer.
- [3] Aringhieri, R., Carello, G., & Morale, D. (2007). Ambulance location through optimization and simulation: the case of Milano urban area. XXXVIII Annual Conference of the Italian Operations Research Society Optimization and Decision Sciences, pp. 1-29.
- [4] Aringhieri, R. (2008). Models for the efficient team planning at emergency medical service of Milano. In: Xie, X., Lorca, F., & Marcon, E. (Eds.), *Operations Research for Health Care Delivery Engineering*, Proceeding of the 33rd international conference on Operational Research Applied to Health Service (ORAHS 2007), pp. 281-288.
- [5] Aringhieri, R. (2009). Composing medical crews with equity and efficiency. *Central European Journal of Operations Research*, 17(3), 343-357.
- [6] Bello, I., Pham, H., Le, Q. V., Norouzi, M. & Bengio, S. (2016). Neural Combinatorial Optimization with Reinforcement Learning. arXiv preprint arXiv:1611.09940.
- [7] Benlic, U., & Hao, J. K. (2011). A Multilevel Memetic Approach for Improving Graph K-Partitions. *IEEE Transactions on Evolutionary Computation*, 15(5), 624-642.
- [8] Cho, C. J. (1998). An equity-efficiency trade-off model for the optimum location of medical care facilities. *Socio-Economic Planning Sciences*, 32(2), 99-112.
- [9] Delgado-Osuna, J. A., Lozano, M., & García-Martínez, C. (2016). An alternative artificial bee colony algorithm with destructive-constructive neighbourhood operator for the problem of composing medical crews. *Information Sciences*, 326, 215-226.
- [10] Falkenauer, E. (1996). A hybrid grouping genetic algorithm for bin packing. *Journal of Heuristics*, 2(1), 5-30.

- [11] Galinier, P., & Hao, J. K. (1999). Hybrid Evolutionary Algorithms for Graph Coloring. *Journal of Combinatorial Optimization*, 3(4), 379-397.
- [12] Galinier, P., Boujbel, Z., & Fernandes, M. C. (2011). An efficient memetic algorithm for the graph partitioning problem. *Annals of Operations Research*, 191(1), 1-22.
- [13] Glover, F., & Laguna, M. (1998). Tabu Search. In: Du, DZ., & Pardalos, P. M. (Eds.), *Handbook of Combinatorial Optimization*, pp. 2093-2229. Boston: Springer.
- [14] Hao, J. K. (2012). Memetic Algorithms in Discrete Optimization. In: Neri, F., Cotta, C., & Moscato, P. (Eds.), *Handbook of Memetic Algorithms, Studies in Computational Intelligence, Vol 379* (pp. 73-94). Berlin: Springer.
- [15] Hong, W., Tang, K., Zhou, A., Ishibuchi, H., & Yao, X. (2018). A scalable indicator-based evolutionary algorithm for large-scale multiobjective optimization. *IEEE Transactions on Evolutionary Computation*, 23(3), 525-537.
- [16] Jin, Y., & Hao, J. K. (2016). Hybrid evolutionary search for the minimum sum coloring problem of graphs. *Information Sciences*, 352-353, 15-34.
- [17] Karaboga, D., Gorkemli, B., Ozturk, C., & Karaboga, N. (2014). A comprehensive survey: artificial bee colony (ABC) algorithm and applications. *Artificial Intelligence Review*, 42(1), 21-57.
- [18] Khodaparasti, S., Maleki, H. R., Bruni, M. E., Jahedi, S., Beraldi, P., & Conforti, D. (2016). Balancing efficiency and equity in location-allocation models with an application to strategic EMS design. *Optimization Letters*, 10(5), 1053-1070.
- [19] Kuhn, H. W. (1955). The Hungarian method for the assignment problem. *Naval Research Logistics Quarterly*, 2(1-2), 83-97.
- [20] Li, Z., Chen, Q., & Koltun, V. (2018). Combinatorial Optimization with Graph Convolutional Networks and Guided Tree Search. In *Advances in Neural Information Processing Systems*, pp. 539-548.
- [21] López-Ibáñez, M., Dubois-Lacoste, J., Cáceres, L. P., Birattari, M., & Stützle, T. (2016). The irace package: Iterated racing for automatic algorithm configuration. *Operations Research Perspectives*, 3, 43-58.
- [22] Mayhew, L. D., & Leonardi, G. (1982). Equity, Efficiency, and Accessibility in Urban and Regional Health-Care Systems. *Environment and Planning A: Economy and Space*, 14(11), 1479-1507.
- [23] Moeini, R., Soltani-nezhad, M., & Daei, M. (2017). Constrained gravitational search algorithm for large scale reservoir operation optimization problem. *Engineering Applications of Artificial Intelligence*, 62, 222-233.
- [24] Moscato, P., & Cotta, C. (2003). A Gentle Introduction to Memetic Algorithms. In: Glover, F., & Kochenberger, G. A. (Eds.), *Handbook of Metaheuristics, International Series in Operations Research & Management Science, Vol 57* (pp. 105-144). Boston: Springer.

- [25] Paraskevopoulos, D. C., Laporte, G., Repoussis, P. P., & Tarantilis, C. D. (2017). Resource constrained routing and scheduling: Review and research prospects. *European Journal of Operational Research*, 263(3), 737-754.
- [26] Porumbel, D. C., Hao, J. K. & Kuntz, P. (2010). An evolutionary approach with diversity guarantee and well-informed grouping recombination for graph coloring. *Computers & Operations Research*, 37(10), 1822-1832.
- [27] Qin, J., Xu, X., Wu, Q., & Cheng, T. C. E. (2016). Hybridization of tabu search with feasible and infeasible local searches for the quadratic multiple knapsack problem. *Computers & Operations Research*, 66, 199-214.
- [28] Rennie, S. J. , Marcheret, E., Mroueh, Y., Ross, J. & Goel, V. (2017). Self-Critical Sequence Training for Image Captioning. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 7008-7024.
- [29] Silva, G. C., Ochi, L. S., & Martins, S. L. (2004). Experimental Comparison of Greedy Randomized Adaptive Search Procedures for the Maximum Diversity Problem. In: Ribeiro, C. C., & Martins S. L. (Eds.), *Experimental and Efficient Algorithms*, Lecture Notes in Computer Science, Vol 3059 (pp. 498-512). Berlin: Springer.
- [30] Smith, H. K., Harper, P. R., & Potts, C. N. (2013). Bicriteria efficiency/equity hierarchical location models for public service application. *Journal of the Operational Research Society*, 64(4), 500-512.
- [31] Sun, W., Hao, J. K., Lai, X., & Wu, Q. (2018). Adaptive feasible and infeasible tabu search for weighted vertex coloring. *Information Sciences*, 466, 203-219.
- [32] Tian, C., Xu, Y., Fei, L., Wang, J., Wen, J., & Luo, N. (2019). Enhanced CNN for image denoising. *CAAI Transactions on Intelligence Technology*, 4(1), 17-23.

Appendix

This appendix shows the pseudo codes of the proposed memetic algorithm (Algorithm 1) and its composing procedures, including the greedy construction procedure (Algorithm 2), the backbone-based crossover operator procedure (Algorithm 3), the tabu search procedure with feasible and infeasible exploration (Algorithms 4-6).

Algorithm 1 Main scheme of MA

- 1: **Input:** An instance I , time limit t_{max} , population size $|P|$
 - 2: **Output:** Best solution S^* found
 - 3: Initialize population $Pop = \{S^1, S^2, \dots, S^{|P|}\}$
 - 4: $S^* \leftarrow Best(Pop)$
 - 5: **while** Time does not exceed t_{max} **do**
 - 6: Select two parents $S^i \in Pop$ and $S^j \in Pop$ at random
 - 7: $S^o \leftarrow Crossover(S^i, S^j)$ /* Crossover to generate an offspring solution, Section 4 */
 - 8: $S^o \leftarrow FITS(S^o)$ /* Improve the offspring solution by the tabu search procedure, Section 5 */
 - 9: **if** $f(S^o) > f(S^*)$ **then**
 - 10: $S^* \leftarrow S^o$ /* Update the recorded best solution */
 - 11: **end if**
 - 12: $Pop \leftarrow Pool_Updating(S^o, Pop)$ /* Update the population, Section 3.3 */
 - 13: **end while**
-

Algorithm 2 The greedy construction algorithm

- 1: **Input:** Instance I
 - 2: **Output:** A feasible initial solution denoted by $S = \{C_0, C_1, \dots, C_T\}$
 - 3: Initializing $C_0 = \{1, \dots, n\}$, $C_t = \emptyset$ ($t \in \{1, \dots, T\}$), $B_{pt} = 0$ ($t \in \{1, \dots, T\}$, $p \in \{1, \dots, n\}$)
 - 4: **repeat**
 - 5: $E_{max} \leftarrow \{p \in C_0 : e_p = \max_{v \in C_0} \{e_v\}\}$ /* E_{max} represents the set of unallocated individuals with the largest efficiency */
 - 6: $S_{min} \leftarrow \{t = 1, \dots, T : |C_t| = \min\{|C_m|, m = 1, \dots, T\}\}$ /* S_{min} denotes the set of crews with the smallest cardinality */
 - 7: select $p \in E_{max}$, $t \in S_{min}$ such that B_{pt} is maximized
 - 8: $C_0 \leftarrow C_0 \setminus \{p\}$
 - 9: $C_t \leftarrow C_t \cup \{p\}$
 - 10: **for** each $q \in \{1, \dots, n\}$ **do**
 - 11: $B_{pt} = B_{pt} + d_{pq}$
 - 12: **end for**
 - 13: **until** Each crew C_t ($t \in \{1, \dots, T\}$) has exactly M_t individuals
 - 14: **if** S is an infeasible solution **then**
 - 15: $repair_solution(S)$ /* Solution repair procedure, Section 5.4 */
 - 16: **end if**
 - 17: **return** $S = \{C_0, C_1, \dots, C_T\}$
-

Algorithm 3 The backbone-based crossover

```
1: Input: Two parent solutions  $S^1 = \{C_0^1, C_1^1, \dots, C_T^1\}$  and  $S^2 = \{C_0^2, C_1^2, \dots, C_T^2\}$ 
2: Output: A feasible offspring solution  $S^o = \{C_0^o, C_1^o, \dots, C_T^o\}$ 
3: /* Step 1: Create a partial solution based on backbone */
4: /* Group matching procedure */
5: Initializing  $C_0^o = \{1, \dots, n\}$ ,  $C_t^o = \emptyset$  ( $t \in \{1, \dots, T\}$ )
6: for  $t := 1$  to  $T$  do
7:   Identify a crew  $C_i^1$  of  $S^1$  and a crew  $C_j^2$  of  $S^2$  ( $i, j \in \{1, \dots, T\}$ ) such
   that  $C_i^1$  and  $C_j^2$  have the maximum number of identical individuals
8:    $C_t^o \leftarrow C_i^1 \cap C_j^2$ 
9:   /* Extending procedure */
10:   $coin \leftarrow 1$ ;  $L_1 \leftarrow C_i^1 \setminus C_t^o$ ;  $L_2 \leftarrow C_j^2 \setminus C_t^o$ 
11:  while  $|C_t^o| < M_t$  && ( $L_1 \neq \emptyset$  or  $L_2 \neq \emptyset$ ) do
12:    if  $coin$  is odd then
13:      Choose an individual  $p$  from  $L_1$  with the highest individual
      contribution
14:    else
15:      Choose an individual  $p$  from  $L_2$  with the highest individual
      contribution
16:    end if
17:     $C_t^o \leftarrow C_t^o \cup \{p\}$ 
18:     $L_1 \leftarrow L_1 \setminus \{p\}$ ;  $L_2 \leftarrow L_2 \setminus \{p\}$ ;  $coin \leftarrow coin + 1$ 
19:  end while
20:  Remove all individuals in  $C_t^o$  from all crews of  $S^1$  and  $S^2$ 
21: end for
22: /* Step 2: complete the partial offspring solution */
23:  $L \leftarrow \{1, \dots, n\} \setminus \{C_1^o \cup \dots \cup C_T^o\}$ 
24: repeat
25:   Identify an individual  $p$  from  $L$  and a crew  $t$  among the ones having the
   smallest cardinality such that the individual contribution  $IC(S^o, p, t)$  is
   maximized
26:    $C_t^o \leftarrow C_t^o \cup \{p\}$ ;  $L \leftarrow L \setminus \{p\}$ 
27: until Each crew  $C_t^o$  ( $t \in \{1, \dots, T\}$ ) has exactly  $M_t$  individuals
28: if  $S^o$  is an infeasible solution then
29:    $repair\_solution(S^o)$  /* Repair the infeasible solution, Section 5.4 */
30: end if
31: return  $S^o$ 
```

Algorithm 4 Main scheme of FITS

```
1: Input: An instance  $I$ , solution  $S$ 
2: Output: Best found feasible solution  $S^*$ 
3: Begin
4:  $S^* \leftarrow S$  /*  $S^*$  records the best feasible solution found so far */
5:  $\beta \leftarrow 0$ 
6: while  $\beta < \beta_{max}$  do
7:   /* feasible local search phase */
8:    $(S^1, S^{local\_best}) \leftarrow feasible\_local\_search(S)$  /* Section 5.2 */
9:   if  $f(S^{local\_best}) > f(S^*)$  then
10:     $S^* \leftarrow S^{local\_best}$  /* Update the best recorded solution */
11:   end if
12:   /* infeasible local search phase */
13:    $(S, S^{local\_best}) \leftarrow infeasible\_local\_search(S^1)$  /* Section 5.3 */
14:   if  $f(S^{local\_best}) > f(S^*)$  then
15:     $S^* \leftarrow S^{local\_best}$ 
16:   end if
17:    $\beta \leftarrow \beta + 1$ 
18: end while
19: return  $S^*$ 
```

Algorithm 5 Feasible Local Search

```
1: Input: Solution  $S$ 
2: Output: Final solution  $S$ , best solution  $S^{local\_best}$  found
3:  $S^{local\_best} \leftarrow S$  /*  $S^{local\_best}$  records the best solution found so far */
4:  $NI \leftarrow 0$  /* number of consecutive iterations without improvement of
    $S^{local\_best}$  */
5: Initialize tabu_list
6: while  $NI < N_{cons}$  do
7:   Choose a best admissible neighboring solution  $S'$ 
8:    $S \leftarrow S'$ 
9:   Update tabu_list
10:  if  $f(S) > f(S^{local\_best})$  then
11:    $S^{local\_best} \leftarrow S$ 
12:    $NI \leftarrow 0$ 
13:  else
14:    $NI \leftarrow NI + 1$ 
15:  end if
16: end while
17: return  $(S, S^{local\_best})$ 
```

Algorithm 6 Infeasible Local Search

```
1: Input: Feasible solution  $S$  returned by the feasible local search phase
2: Output: Final resulting solution  $S$ , best feasible solution found during
   this phase  $S^{local\_best}$ 
3:  $S^{local\_best} \leftarrow S$ 
4:  $MI \leftarrow 0$ 
5:  $\beta \leftarrow 0$ 
6: Initialize tabu_list
7: while  $MI \leq M_{ILS}$  do
8:   Select a best admissible neighboring solution  $S'$  in terms of the extended
   penalty-based evaluation function  $F$ 
9:    $S \leftarrow S'$ 
10:  Update tabu_list
11:  if  $S$  is a feasible solution then
12:    if  $f(S) > f(S^{local\_best})$  then
13:       $S^{local\_best} \leftarrow S$ 
14:    end if
15:  end if
16:   $MI \leftarrow MI + 1$ 
17:  if All previous  $\lambda$  solutions are feasible then
18:     $\beta \leftarrow \beta - 1$ 
19:  else if They are all infeasible solutions then
20:     $\beta \leftarrow \beta + 1$ 
21:  end if
22:  if  $\beta < 0$  then  $\beta \leftarrow 0$  end if
23: end while
24: if  $S$  is not a feasible solution then
25:   repair_solution( $S$ ) /* Solution repair procedure, Section 5.4 */
26: end if
27: return ( $S, S^{local\_best}$ )
```
